# TCC: Differential expression analysis for tag count data with robust normalization strategies

Jianqiang Sun<sup>1§</sup>, Tomoaki Nishiyama<sup>2§</sup>, Kentaro Shimizu<sup>1</sup>, and Koji Kadota<sup>1</sup>

 $^{1}$  The University of Tokyo, Tokyo, Japan

 $^{2}\,$  Kanazawa University, Kanazawa, Japan

§ Maintainer: Jianqiang Sun (sun@biunit.dev),

Tomoaki Nishiyama (tomoakin@staff.kanazawa-u.ac.jp)

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### Abstract

The R/Bioconductor package, **TCC**, provides users with a robust and accurate framework to perform differential expression (DE) analysis of tag count data. We developed a multi-step normalization method (TbT; Kadota et al., 2012) for two-group RNA-seq data. The strategy (called DEGES) is to remove data that are potential differentially expressed genes (DEGs) before performing the data normalization. DEGES in **TCC** is essential for accurate normalization of tag count data, especially when the up-and down-regulated DEGs in one of the groups are extremely biased in their number. A major characteristic of **TCC** is to provide the DEGES-based normalization methods for several kinds of count data (two-group, multi-group, and so on) by virtue of the use of combinations of functions in other sophisticated packages (especially **edgeR**). The appropriate combination provided by **TCC** allows a more robust and accurate estimation to be performed more easily than directly using original packages and **TCC** provides a simple unified interface to perform the robust normalization.

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# 1 Introduction

Differential expression analysis based on tag count data has become a fundamental task for identifying differentially expressed genes or transcripts (DEGs). The **TCC** package (Tag Count Comparison; Sun et al., 2013) provides users with a robust and accurate framework to perform differential expression analysis of tag count data. **TCC** provides integrated analysis pipelines with improved data normalization steps, compared with other packages such as **edgeR** by appropriately combining their functionalities. The package incorporates multistep normalization methods whose strategy is to remove data that are potential DEGs before performing the data normalization.

Kadota et al. (2012) recently reported that the normalization methods implemented in R packages (such as edgeR (Robinson et al., 2010), and DESeq (Anders and Huber, 2010) for differential expression (DE) analysis between samples are inadequate when the up- and down-regulated DEGs in one of the samples are extremely biased in their number (i.e., biased DE). This is because the current methods implicitly assume a balanced DE, wherein the numbers of highly and lowly expressed DE entities in samples are (nearly) equal. As a result, methods assuming unbiased DE will not work well on data with biased DE. Although a major purpose of data normalization is to detect such DE entities, their existence themselves consequently interferes with their opportunity to be top-ranked. Conventional procedures for identifying DEGs from tag count data consisting of two steps (i.e., data normalization and identification of DEGs) cannot in principle eliminate the potential DE entities before data normalization.

To normalize data that potentially has various scenarios (including unbiased and biased DE), we recently proposed a multi-step normalization strategy (called TbT, an acronym for the TMM-baySeq-TMM pipeline; Kadota et al., 2012), in which the TMM normalization method (Robinson and Oshlack, 2010) is used in steps 1 and 3 and an empirical Bayesian method implemented in the baySeq package (Hardcastle and Kelly, 2010) is used in step 2. Although this multi-step DEG elimination strategy (called "DEGES" for short) can successfully remove potential DE entities identified in step 2 prior to the estimation of the normalization factors using the TMM normalization method in step 3, the baySeq package used in step 2 of the TbT method is much more computationally intensive than competing packages like **edgeR** and **DESeq2**. While the three-step TbT normalization method performed best on simulated and real tag count data, it is practically possible to make different choices for the methods in each step. A more comprehensive study regarding better choices for DEGES is needed.

This package provides tools to perform multi-step normalization methods based on DEGES and enables differential expression analysis of tag count data without having to worry much about biased distributions of DEGs. The DEGES-based normalization function implemented in **TCC** includes the TbT method based on DEGES for two-group data, much faster method, and methods for multi-group comparison. **TCC** provides a simple unified interface to perform data normalization with combinations of functions provided by **DESeq2** and **edgeR**. Functions to produce simulation data under various conditions and to plot the data are also provided.

## 1.1 Installation

This package is available from the Bioconductor website (http://bioconductor.org/). To install the package, enter the following command after starting R:

```
> if (!requireNamespace("BiocManager", quietly=TRUE))
> install.packages("BiocManager")
> BiocManager::install("TCC")
```

# 1.2 Citations

This package internally uses many of the functions implemented in the other packages. This is because our normalization procedures consist, in part, of combinations of existing normalization methods and differential expression (DE) methods.

For example, the TbT normalization method (Kadota et al., 2012), which is a particular functionality of the **TCC** package (Sun et al., 2013), consists of the TMM normalization method (Robinson and Oshlack, 2010) implemented in the **edgeR** package (Robinson et al., 2010) and the empirical Bayesian method implemented in the **baySeq** package (Hardcastle and Kelly, 2010). Therefore, please cite the appropriate references when you publish your results.

> citation("TCC")

# 1.3 Quick start

Let us begin by showing a example of identifying DEGs between two groups from tag count data consisting of 1,000 genes and a total of six samples (each group has three biological replicates). The hypothetical count data (termed "hypoData") is stored in this package (for details, see section 2.1).

DE analysis for two-group count data with replicates by using the F-test (see glmQLFTest in edgeR package) coupled with iterative DEGES/edgeR normalization (i.e., the iDEGES/edgeRedgeR combination). This is an alternative pipeline designed to reduce the runtime (approx. 20 sec.), yet its performance is comparable to the above pipeline. Accordingly, we recommend using this pipeline as a default when analyzing tag count data with replicates. A notable advantage of this pipeline is that the multi-step normalization strategy only needs the methods implemented in the edgeR package. The suggested citations are as follows: TCC (Sun et al., 2013), TMM (Robinson and Oshlack, 2010), and edgeR (Robinson et al., 2010). For details, see section 3.1.2 and 4.1.1.

```
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)
> tcc <- new("TCC", hypoData, group)
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 3, FDR = 0.1, floorPDEG = 0.05)
> tcc <- estimateDE(tcc, test.method = "edger", FDR = 0.1)
> result <- getResult(tcc, sort = TRUE)
> head(result)
```

```
p.value
                                               q.value rank estimatedDEG
   gene_id a.value
                    m.value
1 gene_151 9.736230 -2.749909 6.171692e-06 0.001205894
                                                         1
                                                                       1
2 gene_168 8.903595 -1.965453 7.211376e-06 0.001205894
                                                          2
                                                                       1
3 gene_144 7.588262 -2.126825 7.636756e-06 0.001205894
                                                          3
                                                                       1
  gene_11 8.772243 -2.101167 9.538190e-06 0.001205894
                                                          4
                                                                       1
5 gene_123 8.213530 -2.148411 1.058751e-05 0.001205894
                                                          5
                                                                       1
6 gene_143 9.284689 -1.970371 1.074955e-05 0.001205894
                                                          6
                                                                       1
```

#### 2 Preparations

#### 2.1Preparing the count data

Similar to the other packages, **TCC** typically starts the DE analysis with a count table matrix where each row indicates a gene (or transcript), each column indicates a sample (or library), and each cell indicates the number of counts for a gene in a sample. There are many ways to obtain the count data from aligned read files such as BAM (Binary Alignment/Map). This includes the islandCounts function in htSeqTools (Planet et al., 2012). summarizeOverlaps in GenomicRanges (Lawrence et al., 2013), qCount in QuasR, and so on. For Windows end users, we recommend to use the **QuasR** package. It provides a comprehensive workflow for many kinds of NGS data including ChIP-seq, RNA-seq, smallRNA-seq, and BS-seq. The main functionalities are: (1) preprocessing raw sequence reads, (2) aligning reads to the reference genome or transcriptome using **Rbowtie**, and (3) producing count matrix from aligned reads. TCC uses the raw count data (a matrix of integer values) as input. As also clearly mentioned in **DESeq2**, the raw count data corresponds to a matrix of integer values. Please DO NOT use any normalized counts such as RPM (reads per million), CPM (counts per million), and RPKM.

#### 2.2Reading the count data

Here, we assume a hypothetical count matrix consisting of 1,000 rows (or genes) and a total of six columns: the first three columns are produced from biological replicates of Group 1 (G1 rep1, G1 rep2, and G1 rep3) and the remaining columns are from Group 2 (G2 rep1, G2 rep2, and G2 rep3). We start by loading the hypothetical data (hypoData) from TCC and giving a numeric vector (group) indicating which group each sample belongs to.

29

68

239

0

5

69

```
> library(TCC)
> data(hypoData)
> head(hypoData)
       G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2 G2_rep3
                             122
            34
                     45
                                                14
                                       16
gene_1
                     388
                              22
gene_2
            358
                                       36
                                                25
           1144
                     919
                             990
                                      374
                                               480
gene_3
              0
                      0
                              44
                                       18
                                                 0
gene_4
gene_5
             98
                     48
                              17
                                        1
                                                 8
            296
                     282
                                       86
                                                62
gene_6
                             216
> dim(hypoData)
[1] 1000
             6
> group <- c(1, 1, 1, 2, 2, 2)
```

If you want to analyze another count matrix consisting of nine columns (e.g., the first four columns are produced from biological replicates of G1, and the remaining five columns are from G2), the group vector should be indicated as follows.

> group <- c(1, 1, 1, 1, 2, 2, 2, 2, 2)

## 2.3 Constructing TCC class object

The **new** function has to be used to perform the main functionalities of **TCC**. This function constructs a **TCC** class object, and subsequent analyses are performed on this class object. The object is constructed from i) a count matrix (hypoData) and ii) the corresponding numeric vector (group) as follows.

```
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)
> tcc <- new("TCC", hypoData, group)</pre>
> tcc
Count:
       G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2 G2_rep3
                            122
gene_1
           34
                    45
                                      16
                                               14
                                                        29
           358
                    388
                              22
                                      36
                                               25
                                                        68
gene_2
gene_3
          1144
                    919
                             990
                                     374
                                              480
                                                       239
gene_4
             0
                      0
                              44
                                      18
                                                0
                                                        0
                                                8
            98
                     48
                              17
                                                        5
                                      1
gene_5
           296
                    282
                                      86
                                               62
                                                        69
                             216
gene_6
Sample:
        group norm.factors lib.sizes
G1_rep1
            1
                          1
                                142177
G1_rep2
                                145289
            1
                          1
G1_rep3
                                149886
            1
                          1
G2_rep1
            2
                                112100
                          1
            2
G2_rep2
                          1
                                104107
G2_rep3
            2
                           1
                                101975
```

The count matrix and group vector information can be retrieved from the stored class object by using tcc\$count and tcc\$group, respectively.

### > head(tcc\$count)

	G1_rep1	G1_rep2	G1_rep3	G2_rep1	G2_rep2	G2_rep3
gene_1	34	45	122	16	14	29
gene_2	358	388	22	36	25	68
gene_3	1144	919	990	374	480	239
gene_4	0	0	44	18	0	0
gene_5	98	48	17	1	8	5
gene_6	296	282	216	86	62	69

### > tcc\$group

	group
G1_rep1	1
G1_rep2	1
G1_rep3	1
G2_rep1	2
G2_rep2	2
G2_rep3	2

# 2.4 Filtering low-count genes (optional)

The way to filter out genes with low-count tags across samples depends on the user's philosophy. Although we recommend removing tags with zero counts across samples as a minimum filtering, this effort is optional. The filterLowCountGenes function performs this filtering.

```
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)
> tcc <- new("TCC", hypoData, group)
> tcc <- filterLowCountGenes(tcc)
> dim(tcc$count)
```

[1] 996 6

[1] 996

6

It can be seen that 4(= 1000 - 996) genes were filtered as non-expressed. The same procedure can be performed without the filterLowCountGenes function, in which case the filtering is performed before the **TCC** class object is constructed.

```
> filter <- as.logical(rowSums(hypoData) > 0)
> dim(hypoData[filter, ])
[1] 996   6
> tcc <- new("TCC", hypoData[filter, ], group)
> dim(tcc$count)
```

# 3 Normalization

This chapter describes the details of our robust normalization strategy (i.e., DEGES) implemented in **TCC**. Alternative DEGES procedures consisting of functions in other packages (edgeR and DESeq2) are also provided, enabling *advanced* users familiar with the existing packages can easily learn what is done in **TCC**. Note that *end* users, who just want to perform robust differential expression analysis using **TCC**, can skip this chapter (3 Normalization) and move from here to, for example, the next chapter (4 Differential expression). Note also that the purpose here is to obtain accurate normalization factors to be used with statistical models (e.g., the exact test or empirical Bayes) for the DE analysis described in the next section (4 Differential expression). **TCC** can manipulate various kinds of experimental designs. Followings are some examples for individual designs. Appropriate sections should be referred for your specific experimental designs.

Table 1: 3.1 unpaired samples (two-gr	roup	(two-gr	mples	l s	unpaired	3.1	1:	Table
---------------------------------------	------	---------	-------	-----	----------	-----	----	-------

Label	Example 1	Example 2	Label	Example 3	Example 4
G1_rep1	$G1(mouse_A)$	Tumor(patient_A)	G1_rep1	$G1(mouse_A)$	Tumor(patient_A)
G1_rep2	$G1(mouse\_B)$	$Tumor(patient_B)$	G1_rep2	$G1(mouse\_B)$	$Tumor(patient_B)$
G1_rep3	$G1(mouse_C)$	$Tumor(patient_C)$	G2_rep1	$G2(mouse_D)$	Normal(patient_G)
G2_rep1	$G2(mouse_D)$	$Normal(patient_G)$	$G2_{rep2}$	$G2(mouse_E)$	Normal(patient_H)
G2_rep2	$G2(mouse_E)$	Normal(patient_H)			
G2_rep3	$G2(mouse_F)$	$Normal(patient_K)$			

Table 2: 3.2 paired samples (two-group)

Label	Example 1	Example 2	Label	Example 3	Example 4
G1_rep1	$G1(mouse_A)$	Tumor(patient_G)	G1_rep1	$G1(mouse\_B)$	$Tumor(patient_J)$
G1_rep2	$G1(mouse\_B)$	$Tumor(patient_H)$	$G1\_rep2$	$G1(mouse_C)$	$Tumor(patient_K)$
G1_rep3	$G1(mouse_C)$	$Tumor(patient_K)$	$G2\_rep1$	$G2(mouse\_B)$	$Normal(patient_J)$
G2_rep1	$G2(mouse_A)$	$Normal(patient_G)$	$G2_{rep2}$	$G2(mouse_C)$	$Normal(patient_K)$
G2_rep2	$G2(mouse\_B)$	$Normal(patient_H)$			
G2_rep3	$G2(mouse_C)$	$Normal(patient_K)$			

Label	Example 1	Example 2	Label	Example 3	Example 4
G1_rep1	$G1(mouse_A)$	Kidney(sample_A)	G1_rep1	$G1(mouse_A)$	Liver(sample_G)
G1_rep2	$G1(mouse_B)$	$Kidney(sample_B)$	$G1\_rep2$	$G1(mouse_B)$	$Liver(sample_H)$
G1_rep3	$G1(mouse_C)$	Kidney(sample_C)	$G2\_rep1$	$G2(mouse_D)$	$Brain(sample_Y)$
G2_rep1	$G2(mouse_D)$	$Liver(sample_G)$	$G2_{rep2}$	$G2(mouse_E)$	$Brain(sample_Z)$
G2_rep2	$G2(mouse_E)$	Liver(sample_H)	G3_rep1	$G3(mouse_U)$	Kidney(sample_B)
G2_rep3	$G2(mouse_F)$	$Liver(sample_K)$	$G3_{rep2}$	$G3(mouse_T)$	Kidney(sample_C)
G3_rep1	$G3(mouse_G)$	$Brain(sample_X)$			
G3_rep2	$G3(mouse_H)$	$Brain(sample_Y)$			
G3_rep3	$G3(mouse_I)$	$Brain(sample_Z)$			

Table 3: 3.3 unpaired samples (multi-group)

# 3.1 Normalization of two-group count data with replicates

This package provides robust normalization methods based on DEGES proposed by Kadota et al. (2012). When obtaining normalization factors from two-group data with replicates, users can select a total of six combinations (two normalization methods  $\times$  three DEG identification methods) coupled with an arbitrary number of iterations (n = 0, 1, 2, ..., 100) in our DEGES-based normalization pipeline. We show some of the practical combinations below.

Since the three-step TbT normalization method was originally designed for normalizing tag count data with (biological) replicates, we present three shorter alternatives (3.1.1 DEGES/edgeR, 3.1.2 iDEGES/edgeR, and 3.1.3 DEGES/DESeq2).

### 3.1.1 DEGES/edgeR

Now let us describe an alternative approach that is roughly 200-400 times faster than DEGES/TbT, yet has comparable performance. The TMM-edgeR-TMM pipeline (called DEGES/edgeR) employs the exact test implemented in **edgeR** in step 2. To use this pipeline, we have to provide a reasonable threshold for defining potential DEGs in step 2. We will define the threshold as an arbitrary false discovery rate (FDR) with a floor value of  $P_{\text{DEG}}$ . The default FDR is < 0.1, and the default floor  $P_{\text{DEG}}$  is 5%, but different choices are of course possible. For example, in case of the default settings, x%(x > 5%) of the top-ranked potential DEGs are eliminated in step 2 if the percentage (= x%) of genes satisfying FDR < 0.1 is over 5%. The DEGES/edgeR pipeline has an apparent advantage over TbT in computation time. It can be performed as follows:

```
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)
> tcc <- new("TCC", hypoData, group)
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 1, FDR = 0.1, floorPDEG = 0.05)
> tcc$norm.factors
G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2 G2_rep3
0.8803280 0.8598465 0.8433029 1.0845126 1.1439888 1.1880212
```

#### > tcc\$DEGES\$execution.time

user system elapsed 0.277 0.000 0.277

The normalization factors calculated from the DEGES/edgeR are very similar to those of DEGES/TbT with the default parameter settings (i.e., samplesize = 10000). For edgeR users, we provide commands, consisting of functions in edgeR, to perform the DEGES/edgeR pipeline without TCC. The calcNormFactors function together with the above parameter settings can be regarded as a wrapper function for the following commands.

```
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)
> FDR <- 0.1
> floorPDEG <- 0.05</pre>
> d <- DGEList(counts = hypoData, group = group)</pre>
> ### STEP 1 ###
> d <- calcNormFactors(d)</pre>
> ### STEP 2 ###
> design <- model.matrix(~group)</pre>
> d <- estimateDisp(d, design)</pre>
> fit <- glmQLFit(d, design)</pre>
> out <- glmQLFTest(fit, coef = 2)</pre>
> pval <- out$table$PValue</pre>
> qval <- p.adjust(pval, method = "BH")</pre>
> if (sum(qval < FDR) > (floorPDEG * nrow(hypoData))) {
  is.DEG <- as.logical(qval < FDR)</pre>
+ } else {
    is.DEG <- as.logical(rank(pval, ties.method = "min") <=</pre>
+
+
                            nrow(hypoData) * floorPDEG)
+ }
> ### STEP 3 ###
> d <- DGEList(counts = hypoData[!is.DEG, ], group = group)</pre>
> d <- calcNormFactors(d)</pre>
> norm.factors <- d$samples$norm.factors * colSums(hypoData[!is.DEG, ]) /</pre>
                      colSums(hypoData)
> norm.factors <- norm.factors / mean(norm.factors)</pre>
> norm.factors
```

G1\_rep1 G1\_rep2 G1\_rep3 G2\_rep1 G2\_rep2 G2\_rep3 0.8803280 0.8598465 0.8433029 1.0845126 1.1439888 1.1880212

### 3.1.2 iDEGES/edgeR

Our multi-step normalization can be repeated until the calculated normalization factors converge (Kadota et al., 2012). An iterative version of DEGES/TbT (i.e., iDEGES/TbT) can be described as the TMM-(baySeq-TMM)<sub>n</sub> pipeline with  $n \ge 2$ . Although the iDEGES/TbT would not be practical in terms of the computation time, the TMM-(edgeR-TMM)<sub>n</sub> pipeline (iDEGES/edgeR) is potentially superior to both the DEGES/edgeR and the DEGES/TbT. A suggested iDEGES/edgeR implementation (n = 3) consists of seven steps, as follows:

```
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)
> tcc <- new("TCC", hypoData, group)
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 3, FDR = 0.1, floorPDEG = 0.05)
> tcc$norm.factors
```

```
G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2 G2_rep3
0.8706680 0.8501287 0.8389209 1.0844163 1.1491726 1.2066935
> tcc$DEGES$execution.time
    user system elapsed
    0.793 0.000 0.793
```

### 3.1.3 DEGES/DESeq2

The DEGES pipeline can also be performed by using only the functions in the **DESeq2** package. Similar to the **DESeq** case above, this DESeq2-DESeq2-DESeq2 pipeline (DEGES/DESeq2) changes the corresponding arguments of the norm.method and test.method as follows:

```
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)
> tcc <- new("TCC", hypoData, group)
> tcc <- calcNormFactors(tcc, norm.method = "deseq2", test.method = "deseq2",
+ iteration = 1, FDR = 0.1, floorPDEG = 0.05)
> tcc$norm.factors
G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2 G2_rep3
0.8804811 0.8712588 0.8207842 1.0784376 1.1570976 1.1919407
> tcc$DEGES$execution.time
```

```
user system elapsed 3.288 0.000 3.288
```

For **DESeq2** users, we also provide commands, consisting of functions in **DESeq2**, to perform the DEGES/DESeq2 pipeline without **TCC**. The calcNormFactors function together with the above arguments can be regarded as a wrapper function for the following commands.

```
> library(TCC)
> data(hypoData)
> FDR <- 0.1
> floorPDEG <- 0.05</pre>
> group <- factor(c(1, 1, 1, 2, 2, 2))</pre>
> cl <- data.frame(group = group)</pre>
> design <- formula(~ group)</pre>
> dds <- DESeqDataSetFromMatrix(countData = hypoData, colData = cl,</pre>
                                    design = design)
> ### STEP 1 ###
> dds <- estimateSizeFactors(dds)</pre>
> sizeFactors(dds) <- sizeFactors(dds) / mean(sizeFactors(dds))</pre>
> ### STEP 2 ###
> dds <- estimateDispersions(dds)</pre>
> dds <- nbinomWaldTest(dds)</pre>
> result <- results(dds)</pre>
> result$pvalue[is.na(result$pvalue)] <- 1</pre>
> pval <- result$pvalue</pre>
> qval <- p.adjust(pval, method = "BH")</pre>
> if (sum(qval < FDR) > (floorPDEG * nrow(hypoData))) {
```

```
+
  is.DEG <- as.logical(qval < FDR)</pre>
+ } else {
   is.DEG <- as.logical(rank(pval, ties.method = "min") <=</pre>
+
+
                          nrow(hypoData) * floorPDEG)
+ }
> ### STEP 3 ###
> dds <- DESeqDataSetFromMatrix(countData = hypoData[!is.DEG, ], colData = cl,</pre>
                                  design = design)
> dds <- estimateSizeFactors(dds)</pre>
> norm.factors <- sizeFactors(dds) / colSums(hypoData)</pre>
> norm.factors <- norm.factors / mean(norm.factors)</pre>
> norm.factors
  G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2
                                                       G2_rep3
0.8804811 0.8712588 0.8207842 1.0784376 1.1570976 1.1919407
```

# 3.2 Normalization of two-group count data without replicates (paired)

edgeR and DESeq2 employs generalized linear models (GLMs) which can apply to detect DEGs from paired two-group count data. When obtaining normalization factors from paired two group samples, users can select a total of four combinations (two normalization methods  $\times$  two DEG identification methods) coupled with an arbitrary number of iterations  $(n = 0, 1, 2, \dots, 100)$  in our DEGES-based normalization pipeline. The analysis for paired samples can be performed by indicating (1) the pair information when constructing the TCC class object and (2) paired = TRUE when performing the calcNormFactors function. For analyzing paired data, we here use the hypothetical count data (hypoData; for details see 2.2) by changing the label information, i.e.,

	T_dogA	T_dogB	T_dogC	N_dogA	N_dogB	N_dogC
gene_1	34	45	122	16	14	29
gene_2	358	388	22	36	25	68
gene_3	1144	919	990	374	480	239
gene_4	0	0	44	18	0	0
gene_5	98	48	17	1	8	5
gene_6	296	282	216	86	62	69

This count data consists of three individuals (or sibships), dogA, dogB, and dogC. "T" and "N" indicate tumor and normal tissues, respectively.

### 3.2.1 DEGES/edgeR

The DEGES/edgeR pipeline for two-group paired data can be performed as follows:

```
> cl <- data.frame(group = group, pair = pair)
> tcc <- new("TCC", hypoData, cl)
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 1, FDR = 0.1, floorPDEG = 0.05, paired = TRUE)
> tcc$norm.factors
T_dogA T_dogB T_dogC N_dogA N_dogB N_dogC
```

0.8916175 0.8466086 0.8332711 1.0704552 1.1498406 1.2082070

For edgeR users, we provide commands, consisting of functions in edgeR, to perform the DEGES/edgeR pipeline without TCC. The calcNormFactors function together with the above parameter settings can be regarded as a wrapper function for the following commands.

```
> library(TCC)
> data(hypoData)
> colnames(hypoData) <- c("T_dogA", "T_dogB", "T_dogC",
+ "N_dogA", "N_dogB", "N_dogC")
> group <- factor(c(1, 1, 1, 2, 2, 2))
> pair <- factor(c(1, 2, 3, 1, 2, 3))
> design <- model.matrix(~ group + pair)</pre>
> coef <- 2
> FDR <- 0.1
> floorPDEG <- 0.05</pre>
> d <- DGEList(counts = hypoData, group = group)</pre>
> ### STEP 1 ###
> d <- calcNormFactors(d)</pre>
> ### STEP 2 ###
> d <- estimateDisp(d, design)</pre>
> fit <- glmQLFit(d, design)</pre>
> out <- glmQLFTest(fit, coef = coef)</pre>
> pval <- out$table$PValue</pre>
> qval <- p.adjust(pval, method = "BH")</pre>
> if (sum(qval < FDR) > (floorPDEG * nrow(hypoData))){
+
   is.DEG <- as.logical(qval < FDR)</pre>
+ } else {
+
    is.DEG <- as.logical(rank(pval, ties.method = "min") <=</pre>
+
                            nrow(hypoData) * floorPDEG)
+ }
> ### STEP 3 ###
> d <- DGEList(counts = hypoData[!is.DEG, ], group = group)</pre>
> d <- calcNormFactors(d)</pre>
> norm.factors <- d$samples$norm.factors * colSums(hypoData[!is.DEG, ]) /</pre>
+ colSums(hypoData)
> norm.factors <- norm.factors / mean(norm.factors)</pre>
> norm.factors
              T_dogB
                         T_dogC
                                     N_dogA
                                                N_dogB
                                                            N_dogC
   T dogA
0.8916175 0.8466086 0.8332711 1.0704552 1.1498406 1.2082070
```

# 3.3 Normalization of multi-group count data with replicates

Many R packages (including edgeR) support DE analysis for multi-group tag count data. **TCC** provides some prototypes of DEGES-based pipelines for such data. Here, we analyze another hypothetical three-group count matrix, the hypoData\_mg object, provided in **TCC**. It consists of 1,000 genes and a total of nine columns for testing any difference among three groups that each have triplicates.

<pre>&gt; library(TCC) &gt; data(hypoData_mg) &gt; group &lt;- c(1, 1, 1, 2, 2, 2, 3, 3, 3) &gt; tcc &lt;- new("TCC", hypoData_mg, group) &gt; tcc</pre>											
Count:											
	G1_rep1	G1_rep2	G1_rep3	G2_rep1	G2_rep2	G2_rep3	G3_rep1	G3_rep2	G3_rep3		
gene_1	63	48	31	15	12	12	24	15	14		
gene_2	18	0	7	2	3	8	3	5	2		
gene_3	106	66	25	9	14	14	11	11	3		
gene_4	4		6	1	6	1	0	2	2		
gene_5	0	1	2	1	0	1	0	0	1		
gene_6	57	100	83	20	5	16	26	7	21		
Sample:											
		norm.fact									
G1_rep1				150490							
G1_rep2				166665							
G1_rep3				199283							
G2_rep1				183116							
G2_rep2				126651							
G2_rep3				131377							
G3_rep1				149828							
G3_rep2				150288							
G3_rep3	3 3		1 1	141702							

> dim(tcc\$count)

### [1] 1000 9

Of the 1,000 genes, the first 200 genes are DEGs and the remaining 800 genes are non-DEGs. The breakdowns for the 200 DEGs are as follows: 140, 40, and 20 DEGs are upregulated in Groups 1, 2, and 3. Below, we show a DEGES-based normalization pipeline for this multi-group data here.

### 3.3.1 DEGES/edgeR

edgeR employs generalized linear models (GLMs) to find DEGs between any of the groups. The DEGES/edgeR normalization pipeline in **TCC** internally uses functions for the GLM approach that require two models (a full model and a null model). The full model corresponds to a design matrix to describe sample groups. The null model corresponds to the model coefficients. The two models can be defined as follows:

```
> library(TCC)
> data(hypoData_mg)
> group <- c(1, 1, 1, 2, 2, 2, 3, 3, 3)
> tcc <- new("TCC", hypoData_mg, group)
> design <- model.matrix(~ as.factor(group))
> coef <- 2:length(unique(group))</pre>
```

The design matrix (design) can be constructed by using the model.matrix function. For the model coefficients (coef), the user should specify all the coefficients except for the intercept term. The DEGES/edgeR pipeline with the two models (design and coef) can be performed as follows.

```
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 1, design = design, coef = coef)
> tcc$norm.factors
G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2 G2_rep3 G3_rep1 G3_rep2
1.0167505 0.9117014 0.7812211 0.8327624 1.1748081 1.2011016 1.0227500 1.0332822
G3_rep3
1.0256225
```

The two models (design and coef) will automatically be generated when performing the following calcNormFactors function if those models are not explicitly indicated. That is

```
> library(TCC)
> data(hypoData_mg)
> group <- c(1, 1, 1, 2, 2, 2, 3, 3, 3)
> tcc <- new("TCC", hypoData_mg, group)</pre>
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",</pre>
                         iteration = 1)
> tcc$norm.factors
  G1_rep1
            G1_rep2 G1_rep3
                               G2_rep1
                                         G2_rep2
                                                     G2_rep3
                                                                G3_rep1
                                                                          G3_rep2
1.0167505 0.9117014 0.7812211 0.8327624 1.1748081 1.2011016 1.0227500 1.0332822
  G3_rep3
1.0256225
```

For edgeR users, we provide commands, consisting of functions in edgeR, to perform the DEGES/edgeR pipeline without TCC. The calcNormFactors function together with the above parameter settings can be regarded as a wrapper function for the following commands.

```
> library(TCC)
> data(hypoData_mg)
> group <- c(1, 1, 1, 2, 2, 2, 3, 3, 3)
> tcc <- new("TCC", hypoData_mg, group)</pre>
> FDR <- 0.1
> floorPDEG <- 0.05</pre>
> design <- model.matrix(~ as.factor(group))</pre>
> coef <- 2:ncol(design)</pre>
> d <- DGEList(counts = hypoData_mg, group = group)</pre>
> ### STEP 1 ###
> d <- calcNormFactors(d)</pre>
> ### STEP 2 ###
> d <- estimateDisp(d, design)</pre>
> fit <- glmQLFit(d, design)</pre>
> out <- glmQLFTest(fit, coef = coef)</pre>
> result <- as.data.frame(topTags(out, n = nrow(hypoData_mg)))</pre>
> result <- result$table[rownames(hypoData_mg), ]</pre>
> pval <- out$table$PValue</pre>
> qval <- p.adjust(pval, method = "BH")</pre>
> if (sum(qval < FDR) > (floorPDEG * nrow(hypoData_mg))) {
+ is.DEG <- as.logical(qval < FDR)
+ } else {
    is.DEG <- as.logical(rank(pval, ties.method = "min") <=</pre>
+
+
                            nrow(hypoData_mg) * floorPDEG)
+ }
> ### STEP 3 ###
> d <- DGEList(counts = hypoData_mg[!is.DEG, ], group = group)</pre>
> d <- calcNormFactors(d)</pre>
> norm.factors <- d$samples$norm.factors * colSums(hypoData_mg[!is.DEG, ]) /</pre>
                    colSums(hypoData_mg)
> norm.factors <- norm.factors / mean(norm.factors)</pre>
> norm.factors
```

```
G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2 G2_rep3 G3_rep1 G3_rep2
1.0167505 0.9117014 0.7812211 0.8327624 1.1748081 1.2011016 1.0227500 1.0332822
G3_rep3
1.0256225
```

# 3.4 Retrieving normalized data

Similar functions for calculating normalization factors are the calcNormFactors function in edgeR and the estimateSizeFactors function in DESeq2. Note that the terminology used in DESeq2 (i.e., size factors) is different from that used in edgeR (i.e., effective library sizes) and ours. The effective library size in edgeR is calculated as the library size multiplied by the normalization factor. The size factors in both DESeq2 package are comparable to the *normalized* effective library sizes wherein the summary statistics for the effective library sizes are adjusted to one. Our normalization factors, which can be obtained from tcc\$norm.factors, have the same names as those in edgeR. Accordingly, the normalization factors calculated from TCC with arbitrary options should be manipulated together with the library sizes when normalized read counts are to be obtained. Since biologists are often interested in such information (Dillies et al., 2012), we provide the getNormalizedData function for retrieving normalized data.

Note that the hypoData consists of 1,000 genes and a total of six samples (three biological replicates for G1 and three biological replicates for G2); i.e., {G1\_rep1, G1\_rep2, G1\_rep3} vs. {G2\_rep1, G2\_rep2, G2\_rep3}. These simulation data have basically the same conditions as shown in Fig. 1 of the TbT paper (Kadota et al., 2012); i.e., (i) the first 200 genes are DEGs ( $P_{\text{DEG}} = 200/1000 = 20\%$ ), (ii) the first 180 genes of the 200 DEGs are higher in G1 ( $P_{\text{G1}} = 180/200 = 90\%$ ), and the remaining 20 DEGs are higher in G2, and (iii) the level of DE is four-fold. The last 800 genes were designed to be non-DEGs. The different normalization strategies can roughly be evaluated in terms of the similarity of their summary statistics for normalized data labeled as non-DEGs in one group (e.g., G1) to those of the other group (e.g., G2). The basic statistics for the non-DEGs are as follows.

```
> library(TCC)
> data(hypoData)
> nonDEG <- 201:1000</pre>
```

```
> IIOIIDEG <- 201:1000
```

```
> summary(hypoData[nonDEG, ])
```

G1_rep1	G1_rep2	G1_rep3	G2_rep1
Min. : 0.00	Min. : 0	Min. : 0.00	Min. : 0.0
1st Qu.: 3.00	1st Qu.: 4	1st Qu.: 3.00	1st Qu.: 3.0
Median : 20.50	Median : 20	Median : 20.00	Median : 21.0
Mean : 103.36	Mean : 105	Mean : 104.45	Mean : 113.8
3rd Qu.: 74.25	3rd Qu.: 68	3rd Qu.: 73.25	3rd Qu.: 68.0
Max. :8815.00	Max. :9548	Max. :8810.00	Max. :9304.0
G2_rep2	G2_rep3		
Min. : 0 M	in. : 0.0		
1st Qu.: 3 1	st Qu.: 3.0		
Median : 21 M	edian : 20.0		
Mean : 105 M	ean : 104.6		
3rd Qu.: 70 3	rd Qu.: 70.0		
Max. :9466 M	ax. :9320.0		

From now on, we will display only the median values for simplicity, i.e.,

```
> apply(hypoData[nonDEG, ], 2, median)
```

G1\_rep1 G1\_rep2 G1\_rep3 G2\_rep1 G2\_rep2 G2\_rep3 20.5 20.0 20.0 21.0 21.0 20.0

In what follows, we show detailed examples using hypoData. Note, however, that the basic usage is simple.

```
> normalized.count <- getNormalizedData(tcc)</pre>
```

### 3.4.1 Retrieving two-group DEGES/edgeR-normalized data with replicates

The getNormalizedData function can be applied to the TCC class object after the normalization factors have been calculated. The DEGES/edgeR-normalized data can be retrieved as follows.

#### [1] 19.47024 21.69720

For comparison, the summary statistics for TMM-normalized data produced using the original normalization method (i.e., TMM) in **edgeR** can be obtained as follows.

[1] 18.59060 22.98591

It is obvious that the summary statistics (ranging from 19.47024 to 21.69720) from DEGES/edgeR-normalized data are closer to the truth (i.e., ranging from 20.0 to 21.0) than those (ranging from 18.59060 to 22.98591 from TMM-normalized data.

# 3.4.2 Retrieving two-group DEGES/edgeR-normalized data without replicates (paired)

We here analyze the hypoData object provided in TCC. As described in 3.2, we regard hypoData as a hypothetical paired data. The DEGES/edgeR-normalized data can be re-trieved as follows.

```
> library(TCC)
> data(hypoData)
> colnames(hypoData) <- c("T_dogA", "T_dogB", "T_dogC"</pre>
                           "N_dogA", "N_dogB", "N_dogC")
> nonDEG <- 201:1000
> group <- c(1, 1, 1, 2, 2, 2)
> pair <- c(1, 2, 3, 1, 2, 3)
> cl <- data.frame(group = group, pair = pair)</pre>
> tcc <- new("TCC", hypoData, cl)</pre>
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",</pre>
                         iteration = 1, FDR = 0.1, floorPDEG = 0.05, paired = TRUE)
> normalized.count <- getNormalizedData(tcc)</pre>
> head(normalized.count, n = 4)
           T_dogA
                     T_dogB
                               T_dogC
                                         N_dogA
                                                   N_dogB
                                                              N_dogC
         32.97064 44.97317 120.07949 16.39088 14.37695 28.93472
gene 1
gene_2 347.16147 387.76865 21.65368 36.87948 25.67313 67.84694
gene_3 1109.36514 918.45203 974.41555 383.13682 492.92410 238.46204
          0.00000
                   0.00000 43.30736 18.43974
                                                  0.00000
                                                            0.00000
gene_4
> apply(normalized.count[nonDEG, ], 2, median)
 T_dogA
          T_dogB
                    T_dogC
                             N_dogA
                                     N_dogB
                                               N_dogC
19.87936 19.98807 19.68516 21.51303 21.56543 19.95498
> range(apply(normalized.count[nonDEG, ], 2, median))
```

[1] 19.68516 21.56543

For comparison, the summary statistics for TMM-normalized data produced using the original normalization method (i.e., TMM) in **edgeR** can be obtained as follows.

```
> library(TCC)
> data(hypoData)
> colnames(hypoData) <- c("T_dogA", "T_dogB", "T_dogC",</pre>
                            "N_dogA", "N_dogB", "N_dogC")
> nonDEG <- 201:1000
> group <- factor(c(1, 1, 1, 2, 2, 2))</pre>
> d <- DGEList(counts = hypoData, group = group)</pre>
> d <- calcNormFactors(d)</pre>
> norm.factors <- d$samples$norm.factors</pre>
> effective.libsizes <- colSums(hypoData) * norm.factors</pre>
> normalized.count <- sweep(hypoData, 2,</pre>
                              mean(effective.libsizes) / effective.libsizes, "*")
> apply(normalized.count[nonDEG, ], 2, median)
  T_dogA
           T_dogB
                     T_dogC
                               N_dogA
                                        N_dogB
                                                  N_dogC
19.35893 19.01078 18.59060 22.98591 22.16273 21.00685
> range(apply(normalized.count[nonDEG, ], 2, median))
```

[1] 18.59060 22.98591

It is obvious that the summary statistics (ranging from 19.68516 to 21.56543) from DEGES/edgeR-normalized data are closer to the truth (i.e., ranging from 20.0 to 21.0) than those (ranging from 18.59060 to 22.98591) from TMM-normalized data.

### 3.4.3 Retrieving multi-group iDEGES/edgeR-normalized data with replicates

Here, we analyze another hypothetical three-group count matrix, the hypoData\_mg object, provided in TCC. It consists of 1,000 genes and a total of nine columns for testing any difference among three groups that each have triplicates. Similar to the hypoData object, the first 200 genes are DEGs and the remaining 800 genes are non-DEGs. The basic statistics for the non-DEGs are as follows.

> library(TCC)
> data(hypoData\_mg)
> nonDEG <- 201:1000</pre>

> summary(hypoData\_mg[nonDEG, ])

G1_rep1	G1_rep2	G1_rep3	G2_rep1
Min. : 0.00	Min. : 0.0	Min. : 0.0	Min. : 0.0
1st Qu.: 2.00	1st Qu.: 2.0	1st Qu.: 2.0	1st Qu.: 2.0
Median : 14.00	Median : 13.0	Median : 14.5	Median : 13.0
Mean : 135.41	Mean : 150.5	Mean : 190.6	Mean : 199.4
3rd Qu.: 51.25	3rd Qu.: 53.0	3rd Qu.: 55.0	3rd Qu.: 52.0
Max. :27218.00	Max. :27987.0	Max. :66273.0	Max. :75148.0
G2_rep2			
Min. : 0.00	Min. : 0.0	Min. : 0	Min. : 0.0
1st Qu.: 2.00	1st Qu.: 2.0	1st Qu.: 2	1st Qu.: 2.0
Median : 13.00	Median : 14.0	Median : 14	Median : 15.0
Mean : 132.53	Mean : 138.4		
3rd Qu.: 52.25	3rd Qu.: 55.0	3rd Qu.: 52	3rd Qu.: 55.0
Max. :22381.00	Max. :24979.0	Max. :49398	Max. :49709.0
G3_rep3			
Min. : 0.0			
1st Qu.: 2.0			
Median : 15.0			
Mean : 152.1			
3rd Qu.: 50.0			
Max. :39299.0			

From now on, we will display only the median values for simplicity, i.e.,

```
> apply(hypoData_mg[nonDEG, ], 2, median)
```

```
G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2 G2_rep3 G3_rep1 G3_rep2 G3_rep3
14.0 13.0 14.5 13.0 13.0 14.0 14.0 15.0 15.0
```

The iDEGES/edgeR-normalized data can be retrieved as follows.

```
> library(TCC)
> data(hypoData_mg)
> nonDEG <- 201:1000
> group <- c(1, 1, 1, 2, 2, 2, 3, 3, 3)
> tcc <- new("TCC", hypoData_mg, group)
> design <- model.matrix(~ as.factor(group))
> coef <- 2:length(unique(group))
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 3)
> normalized.count <- getNormalizedData(tcc)
> apply(normalized.count[nonDEG, ], 2, median)
G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2 G2_rep3 G3_rep1 G3_rep2
13.98572 13.09136 14.19500 12.99153 13.29936 13.51934 13.96559 14.73326
G3_rep3
15.78603
```

```
> range(apply(normalized.count[nonDEG, ], 2, median))
```

### [1] 12.99153 15.78603

For comparison, the summary statistics for TMM-normalized data produced using the original normalization method (i.e., TMM) in **edgeR** are obtained as follows.

```
> range(apply(normalized.count[nonDEG, ], 2, median))
```

### [1] 19.69837 21.12359

It is obvious that the summary statistics (ranging from 12.99153 to 15.78603) from iDEGES/edgeR-normalized data are closer to the truth (i.e., ranging from 13.0 to 15.0) than those (ranging from 19.69837 to 21.12359) from TMM-normalized data.

# 4 Differential expression (DE)

The particular feature of **TCC** is that it calculates robust normalization factors. Moreover, end users would like to have some accessory functions for subsequent analyses. Here, we provide the estimateDE function for identifying DEGs. Specifically, the function internally uses the corresponding functions implemented in three packages. Similar to the usage in the calcNormFactors function with the test.method argument in **TCC**, those DE methods in edgeR can be performed by using the estimateDE function with test.method = "edger", and "deseq2", respectively. Here, we show some examples of DE analysis for two-group data without replicates (4.1), two-group data with replicates (2.2), and multi-group data with replicates (4.3).

# 4.1 DE analysis for two-group data with replicates

### 4.1.1 edgeR coupled with iDEGES/edgeR normalization

We give a procedure for DE analysis using the exact test implemented in **edgeR** together with iDEGES/edgeR normalization factors (i.e., the iDEGES/edgeR-edgeR combination) for the hypothetical two-group count data with replicates (i.e., the hypoData object). If the user wants to determine the genes having an FDR threshold of < 10% as DEGs, one can do as follows.

```
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)
> tcc <- new("TCC", hypoData, group)
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 3, FDR = 0.1, floorPDEG = 0.05)
> tcc <- estimateDE(tcc, test.method = "edger", FDR = 0.1)</pre>
```

The results of the DE analysis are stored in the **TCC** class object. The summary statistics for top-ranked genes can be retrieved by using the getResult function.

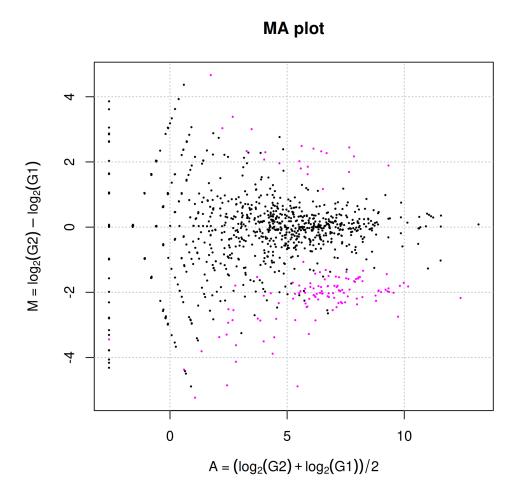
```
> result <- getResult(tcc, sort = TRUE)</pre>
> head(result)
                                               q.value rank estimatedDEG
   gene_id a.value m.value
                                   p.value
1 gene_151 9.736230 -2.749909 6.171692e-06 0.001205894
                                                        1
                                                                       1
2 gene_168 8.903595 -1.965453 7.211376e-06 0.001205894
                                                          2
                                                                       1
3 gene_144 7.588262 -2.126825 7.636756e-06 0.001205894
                                                          3
                                                                       1
  gene_11 8.772243 -2.101167 9.538190e-06 0.001205894
                                                          4
                                                                       1
5 gene_123 8.213530 -2.148411 1.058751e-05 0.001205894
                                                          5
                                                                       1
6 gene_143 9.284689 -1.970371 1.074955e-05 0.001205894
                                                          6
                                                                       1
```

The DE results can be broken down as follows.

```
> table(tcc$estimatedDEG)
```

0 1 864 136

This means 864 non-DEGs and 136 DEGs satisfy FDR < 0.1. The plot function generates an M-A plot, where "M" indicates the log-ratio (i.e.,  $M = \log_2 G2 - \log_2 G1$ ) and "A" indicates average read count (i.e.,  $A = (\log_2 G2 + \log_2 G1)/2$ ), from the normalized count data. The magenta points indicate the identified DEGs at FDR < 0.1.



Since we know the true information for hypoData (i.e., 200 DEGs and 800 non-DEGs), we can calculate the area under the ROC curve (i.e., AUC;  $0 \le AUC \le 1$ ) between the ranked gene list and the truth and thereby evaluate the sensitivity and specificity simultaneously. A well-ranked gene list should have a high AUC value (i.e., high sensitivity and specificity).

```
> library(ROC)
> truth <- c(rep(1, 200), rep(0, 800))
> AUC(rocdemo.sca(truth = truth, data = -tcc$stat$rank))
```

[1] 0.8901719

For comparison, the DE results from the original procedure in **edgeR** can be obtained as follows.

```
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)
> design <- model.matrix(~ as.factor(group))
> d <- DGEList(count = hypoData, group = group)
> d <- calcNormFactors(d)
> d <- estimateDisp(d, design)
> fit <- glmQLFit(d, design)
> out <- glmQLFTest(fit, coef = 2)
> result <- as.data.frame(topTags(out, n = nrow(hypoData), sort.by = "PValue"))
> head(result)
```

```
F
             logFC
                                           PValue
                                                          FDR
                     logCPM
gene_151 -2.600049 13.268812 87.10730 9.983988e-06 0.001866111
gene_168 -1.820356 12.186563 83.34008 1.184851e-05 0.001866111
gene_144 -1.979306 10.925554 80.86171 1.332824e-05 0.001866111
gene_189 2.545458 9.661868 80.60167 1.367049e-05 0.001866111
gene_63 -2.034186 15.740774 78.91067 1.462099e-05 0.001866111
gene_11 -1.956550 12.094762 78.17034 1.516423e-05 0.001866111
```

This is the same as

```
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)</pre>
> tcc <- new("TCC", hypoData, group)</pre>
> tcc <- calcNormFactors(tcc, norm.method = "tmm", iteration = 0)</pre>
> tcc <- estimateDE(tcc, test.method = "edger", FDR = 0.1)</pre>
> result <- getResult(tcc, sort = TRUE)</pre>
> head(result)
                                                q.value rank estimatedDEG
   gene_id a.value
                     m.value
                                   p.value
1 gene_151 9.740529 -2.600366 9.983988e-06 0.001866111 1 1
                                                          2
2 gene_168 8.905896 -1.820884 1.184851e-05 0.001866111
3 gene_144 7.591264 -1.980620 1.332824e-05 0.001866111 3
4 gene_189 6.127498 2.550316 1.367049e-05 0.001866111
                                                          4
5 gene_63 12.402707 -2.034277 1.462099e-05 0.001866111
                                                          5
6
  gene_11 8.774575 -1.957134 1.516423e-05 0.001866111
                                                          6
```

```
> AUC(rocdemo.sca(truth = truth, data = -tcc$stat$rank))
```

[1] 0.8723344

The results of the DE analysis are stored in the TCC class object. The summary statistics for top-ranked genes can be retrieved by using the getResult function.

1

1

1

1

1

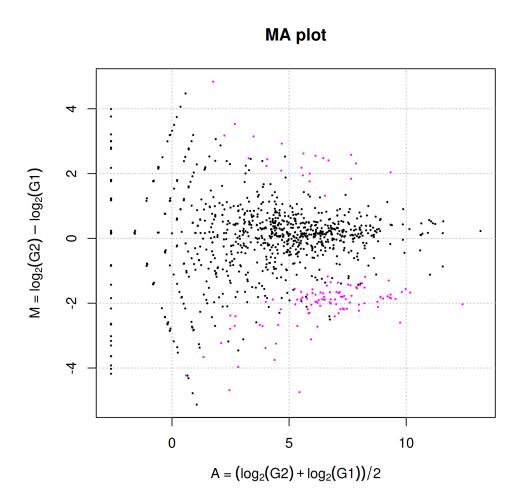
```
> result <- getResult(tcc, sort = TRUE)</pre>
> head(result)
   gene_id a.value
                       m.value
                                       p.value
                                                     q.value rank estimatedDEG
1 gene_151 9.740529 -2.600366 9.983988e-06 0.001866111
                                                              1
                                                                               1
2 gene_168 8.905896 -1.820884 1.184851e-05 0.001866111
                                                                2
                                                                               1
3 gene_144 7.591264 -1.980620 1.332824e-05 0.001866111
4 gene_189 6.127498 2.550316 1.367049e-05 0.001866111
                                                                3
                                                                               1
                                                                4
                                                                               1
5
   gene_63 12.402707 -2.034277 1.462099e-05 0.001866111
                                                                5
                                                                               1
6
   gene_11 8.774575 -1.957134 1.516423e-05 0.001866111
                                                                6
                                                                               1
```

The DE results can be broken down as follows.

```
> table(tcc$estimatedDEG)
```

0 1 876 124

This means 876 non-DEGs and 124 DEGs satisfy FDR < 0.1. The plot function generates an M-A plot, where "M" indicates the log-ratio (i.e.,  $M = \log_2 G2 - \log_2 G1$ ) and "A" indicates average read count (i.e.,  $A = (\log_2 G2 + \log_2 G1)/2$ ), from the normalized count data. The magenta points indicate the identified DEGs at FDR < 0.1.



Since we know the true information for hypoData (i.e., 200 DEGs and 800 non-DEGs), we can calculate the area under the ROC curve (i.e., AUC;  $0 \le AUC \le 1$ ) between the ranked gene list and the truth and thereby evaluate the sensitivity and specificity simultaneously. A well-ranked gene list should have a high AUC value (i.e., high sensitivity and specificity).

```
> library(ROC)
> truth <- c(rep(1, 200), rep(0, 800))
> AUC(rocdemo.sca(truth = truth, data = -tcc$stat$rank))
```

[1] 0.8723344

# ${\bf 4.1.2} \quad {\bf DESeq2} \ coupled \ with \ i {\bf DEGES}/{\bf DESeq2} \ normalization$

For comparison, the DE results from the original procedure in **DESeq2** can be obtained as follows.

```
> library(TCC)
> data(hypoData)
> group <- factor(c(1, 1, 1, 2, 2, 2))
> cl <- data.frame(group = group)
> design <- formula(~ group)</pre>
```

```
> dds <- DESeqDataSetFromMatrix(countData = hypoData, colData = cl,</pre>
                                 design = design)
> dds <- estimateSizeFactors(dds)</pre>
> sizeFactors(dds) <- sizeFactors(dds) / mean(sizeFactors(dds))</pre>
> dds <- estimateDispersions(dds)</pre>
> dds <- nbinomWaldTest(dds)</pre>
> result <- results(dds)</pre>
> head(result[order(result$pvalue),])
log2 fold change (MLE): group 2 vs 1
Wald test p-value: group 2 vs 1
DataFrame with 6 rows and 6 columns
         baseMean log2FoldChange
                                       lfcSE
                                                 stat
                                                             pvalue
                                                                           padj
                     <numeric> <numeric> <numeric>
         <numeric>
                                                         <numeric>
                                                                      <numeric>
         577.362
                         -1.81130 0.188923 -9.58750 9.02463e-22 7.58971e-19
gene_168
         239.748
                         -1.97304 0.220284
-1.94638 0.230809
                                              -8.95678 3.34295e-19 1.40571e-16
gene_144
gene_11
           541.281
                                              -8.43287 3.37280e-17 9.45507e-15
                         -1.81641 0.218271
                                             -8.32181 8.66293e-17 1.82138e-14
gene_143
           752.478
                         -1.78980 0.216748 -8.25749 1.48766e-16 2.50224e-14
           574.796
gene_115
                         -1.72650 0.214623 -8.04432 8.67290e-16 1.21565e-13
gene_109 763.275
> library(ROC)
> truth <- c(rep(1, 200), rep(0, 800))
> result$pvalue[is.na(result$pvalue)] <- 1</pre>
> AUC(rocdemo.sca(truth = truth, data = -rank(result$pvalue)))
[1] 0.8632313
   This is the same as
> library(TCC)
> data(hypoData)
> group <- c(1, 1, 1, 2, 2, 2)
> tcc <- new("TCC", hypoData, group)</pre>
> tcc <- calcNormFactors(tcc, norm.method = "deseq2", iteration = 0)</pre>
> tcc <- estimateDE(tcc, test.method = "deseq2", FDR = 0.1)</pre>
> result <- getResult(tcc, sort = TRUE)</pre>
> head(result)
   gene_id a.value m.value
                                    p.value
                                                 q.value rank estimatedDEG
1 gene_168 8.905999 -1.811262 9.024627e-22 9.024627e-19
                                                           1
                                                                          1
2 gene_144 7.591478 -1.973100 3.342948e-19 1.671474e-16
                                                             2
                                                                          1
3 gene_11 8.774276 -1.946228 3.372796e-17 1.124265e-14
                                                             3
                                                                          1
4 gene_143 9.286710 -1.816512 8.662935e-17 2.165734e-14
                                                          4
                                                                          1
5 gene_115 8.905535 -1.789730 1.487657e-16 2.975314e-14
                                                           5
                                                                          1
6 gene_109 9.331890 -1.726446 8.672896e-16 1.445483e-13
                                                            6
                                                                          1
> library(ROC)
> truth <- c(rep(1, 200), rep(0, 800))
> AUC(rocdemo.sca(truth = truth, data = -tcc$stat$rank))
[1] 0.8632219
```

```
> tcc$norm.factors
```

G1\_rep1 G1\_rep2 G1\_rep3 G2\_rep1 G2\_rep2 G2\_rep3 0.9271692 0.9147550 0.8753592 1.0217885 1.1069052 1.1540229

As described in 3.4, the size factors termed in **DESeq2** is comparable to the *normalized* effective library sizes termed in **TCC** and **edgeR**. The effective library size in **edgeR** is calculated as the library size multiplied by the normalization factor. The normalization factors and effective library sizes in **DESeq2** can be retrieved as follows.

```
> library(TCC)
> data(hypoData)
> group <- factor(c(1, 1, 1, 2, 2, 2))</pre>
> cl <- data.frame(group = group)</pre>
> design <- formula(~ group)</pre>
> dds <- DESeqDataSetFromMatrix(countData = hypoData, colData = cl,</pre>
                                  design = design)
> dds <- estimateSizeFactors(dds)</pre>
> size.factors <- sizeFactors(dds)</pre>
> size.factors
 G1_rep1 G1_rep2 G1_rep3
                                 G2_rep1 G2_rep2
                                                       G2_rep3
1.0830730 1.0919605 1.0779951 0.9411006 0.9468033 0.9668911
> hoge <- size.factors / colSums(hypoData)</pre>
> norm.factors <- hoge / mean(hoge)</pre>
> norm.factors
 G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2
                                                     G2_rep3
0.9271692 0.9147550 0.8753592 1.0217885 1.1069052 1.1540229
> ef.libsizes <- norm.factors * colSums(hypoData)</pre>
> ef.libsizes
 G1_rep1 G1_rep2 G1_rep3 G2_rep1 G2_rep2 G2_rep3
```

Note that the following commands should be the simplest procedure provided in **DESeq2**.

131822.1 132903.8 131204.1 114542.5 115236.6 117681.5

```
log2 fold change (MLE): group 2 vs 1
Wald test p-value: group 2 vs 1
DataFrame with 6 rows and 6 columns
         baseMean log2FoldChange
                                     lfcSE
                                               stat
                                                           pvalue
                                                                         padj
         <numeric>
                       <numeric> <numeric> <numeric>
                                                        <numeric>
                                                                    <numeric>
                        -1.81130 0.188923 -9.58750 9.02463e-22 7.58971e-19
gene_168
         577.362
          239.748
                        -1.97304 0.220284 -8.95678 3.34295e-19 1.40571e-16
gene_144
          541.281
                        -1.94638 0.230809 -8.43287 3.37280e-17 9.45507e-15
gene_11
gene_143
          752.478
                        -1.81641
                                  0.218271
                                            -8.32181 8.66293e-17 1.82138e-14
gene_115
          574.796
                         -1.78980
                                  0.216748
                                             -8.25749 1.48766e-16 2.50224e-14
gene_109
          763.275
                        -1.72650 0.214623
                                            -8.04432 8.67290e-16 1.21565e-13
> library(ROC)
> truth <- c(rep(1, 200), rep(0, 800))
> result$pvalue[is.na(result$pvalue)] <- 1</pre>
> AUC(rocdemo.sca(truth = truth, data = -rank(result$pvalue)))
```

```
[1] 0.8632313
```

# 4.2 DE analysis for two-group data without replicates (paired)

edgeR and DESeq2 employs generalized linear models (GLMs) which can apply to detect DEGs from paired two-group count data. The analysis for paired samples can be performed by indicating (1) the pair information when constructing the TCC class object and (2) paired = TRUE when performing the calcNormFactors and estimateDE functions. For analyzing paired data, we here use the hypothetical count data (hypoData; for details see 2.2) by changing the label information, i.e.,

	T_dogA	$T_dogB$	T_dogC	N_dogA	N_dogB	N_dogC
gene_1	34	45	122	16	14	29
gene_2	358	388	22	36	25	68
gene_3	1144	919	990	374	480	239
gene_4	0	0	44	18	0	0
gene_5	98	48	17	1	8	5
gene_6	296	282	216	86	62	69

This count data consists of three individuals (or sibships), dogA, dogB, and dogC. "T" and "N" indicate tumor and normal tissues, respectively.

We give a procedure for DE analysis using the likelihood ratio test for GLMs implemented in **edgeR** together with iDEGES/edgeR normalization factors (i.e., the iDEGES/edgeRedgeR combination) for the paired two-group count data without replicates (i.e., the above hypoData object). If the user wants to determine the genes having an FDR threshold of < 10% as DEGs, one can do as follows.

```
> cl <- data.frame(group = group, pair = pair)
> tcc <- new("TCC", hypoData, cl)
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 3, FDR = 0.1, floorPDEG = 0.05, paired = TRUE)
> tcc <- estimateDE(tcc, test.method = "edger", FDR = 0.1, paired = TRUE)</pre>
```

The results of the DE analysis are stored in the TCC class object. The summary statistics for top-ranked genes can be retrieved by using the getResult function.

```
> result <- getResult(tcc, sort = TRUE)
> head(result)
```

q.value rank estimatedDEG gene\_id a.value m.value p.value 1 gene\_151 9.737803 -2.748750 1.831973e-05 0.008184452 1 1 2 gene\_63 12.401791 -2.173985 3.814670e-05 0.008184452 2 1 3 3 gene\_68 6.209074 -2.861730 5.711843e-05 0.008184452 1 4 gene\_11 8.772408 -2.099626 6.235542e-05 0.008184452 4 1 5 gene\_105 9.350474 -1.990018 6.857857e-05 0.008184452 5 1 gene\_16 7.348146 -2.339941 8.173766e-05 0.008184452 6 1

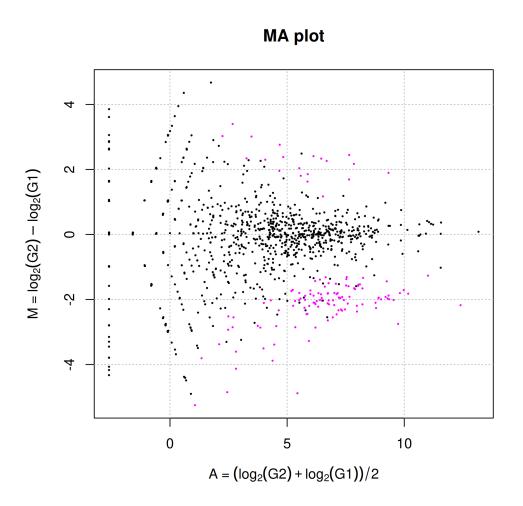
The DE results can be broken down as follows.

```
> table(tcc$estimatedDEG)
```

### 0 1 870 130

This means 870 non-DEGs and 130 DEGs satisfy FDR < 0.1. The plot function generates an M-A plot, where "M" indicates the log-ratio (i.e.,  $M = \log_2 G2 - \log_2 G1$ ) and "A" indicates average read count (i.e.,  $A = (\log_2 G2 + \log_2 G1)/2$ ), from the normalized count data. The magenta points indicate the identified DEGs at FDR < 0.1.

> plot(tcc)



Since we know the true information for hypoData (i.e., 200 DEGs and 800 non-DEGs), we can calculate the area under the ROC curve (i.e., AUC;  $0 \le AUC \le 1$ ) between the ranked gene list and the truth and thereby evaluate the sensitivity and specificity simultaneously. A well-ranked gene list should have a high AUC value (i.e., high sensitivity and specificity).

```
> library(ROC)
> truth <- c(rep(1, 200), rep(0, 800))
> AUC(rocdemo.sca(truth = truth, data = -tcc$stat$rank))
```

[1] 0.8865156

For comparison, the DE results from the original procedure in **edgeR** can be obtained as follows.

```
> library(TCC)
>
  data(hypoData)
  colnames(hypoData) <- c("T_dogA", "T_dogB", "T_dogC",</pre>
>
                                "N_dogA", "N_dogB", "N_dogC")
 group <- factor(c(1, 1, 1, 2, 2, 2))
pair <- factor(c(1, 2, 3, 1, 2, 3))</pre>
>
>
> design <- model.matrix(~ group + pair)</pre>
> coef <- 2
> d <- DGEList(counts = hypoData, group = group)</pre>
> d <- calcNormFactors(d)</pre>
> d <- estimateDisp(d, design)</pre>
 fit <- glmQLFit(d, design)</pre>
>
  out <- glmQLFTest(fit, coef=2)</pre>
>
> topTags(out, n = 6)
```

Coefficient: group2 logCPM logFC F **PValue** FDR gene\_151 -2.572328 13.268838 104.72305 2.601949e-05 0.0114982 gene\_63 -2.073032 15.740778 80.41071 5.940205e-05 0.0114982 gene\_68 -2.759644 9.808735 74.36139 7.659929e-05 0.0114982 gene\_196 2.503385 9.964259 68.95614 9.583007e-05 0.0114982 gene\_11 -1.953234 12.094808 67.50256 1.018457e-04 0.0114982 gene\_189 2.539097 9.661587 67.52002 1.024601e-04 0.0114982 > p.value <- out\$table\$PValue</pre> > library(ROC) > truth <- c(rep(1, 200), rep(0, 800)) > AUC(rocdemo.sca(truth = truth, data = -rank(p.value))) [1] 0.8674469 This is the same as > library(TCC) > data(hypoData) > colnames(hypoData) <- c("T\_dogA", "T\_dogB", "T\_dogC",</pre> "N\_dogA", "N\_dogB", "N\_dogC") > group <- c(1, 1, 1, 2, 2, 2) > pair <- c(1, 2, 3, 1, 2, 3) > cl <- data.frame(group = group, pair = pair)</pre> > tcc <- new("TCC", hypoData, cl)</pre> > tcc <- calcNormFactors(tcc, norm.method = "tmm", iteration = 0, paired = TRUE) > tcc <- estimateDE(tcc, test.method = "edger", FDR = 0.1, paired = TRUE)</pre> > result <- getResult(tcc, sort = TRUE)</pre> > head(result) q.value rank estimatedDEG gene\_id a.value m.value p.value 1 gene\_151 9.740529 -2.600366 2.601949e-05 0.0114982 1 1 2 gene\_63 12.402707 -2.034277 5.940205e-05 0.0114982 2 1 3 gene\_68 6.209636 -2.723799 7.659929e-05 0.0114982 3 1 4 gene\_196 6.461462 2.475704 9.583007e-05 0.0114982 4 1 5 gene\_11 8.774575 -1.957134 1.018457e-04 0.0114982 5 1 6 gene\_189 6.127498 2.550316 1.024601e-04 0.0114982 6 1 > library(ROC) > truth <- c(rep(1, 200), rep(0, 800)) > AUC(rocdemo.sca(truth = truth, data = -tcc\$stat\$rank))

```
[1] 0.8674469
```

## 4.3 DE analysis for multi-group data with replicates

Here, we give three examples of DE analysis coupled with DEGES/edgeR normalization for the hypothetical three-group data with replicates, i.e., the hypoData\_mg object. The use of the DEGES/edgeR normalization factors is simply for reducing the computation time.

### 4.3.1 edgeR coupled with DEGES/edgeR normalization

The exact test implemented in **edgeR** after executing the DEGES/edgeR normalization (i.e., the DEGES/edgeR-edgeR combination) can be performed as follows.

```
> library(TCC)
> data(hypoData_mg)
> group <- c(1, 1, 1, 2, 2, 2, 3, 3, 3)
> tcc <- new("TCC", hypoData_mg, group)</pre>
> ### Normalization ###
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",</pre>
                          iteration = 1)
> ### DE analysis ###
> tcc <- estimateDE(tcc, test.method = "edger", FDR = 0.1)</pre>
> result <- getResult(tcc, sort = TRUE)</pre>
> head(result)
                                               q.value rank estimatedDEG
   gene_id a.value m.value
                                 p.value
                NA
                        NA 2.423134e-07 8.386993e-05
1 gene_140
                                                         1
                                                                        1
                         NA 2.446703e-07 8.386993e-05
2 gene_121
                NA
                                                          2
                                                                        1
3
   gene_64
                NA
                         NA 3.292554e-07 8.386993e-05
                                                          3
                                                                        1
                         NA 3.354797e-07 8.386993e-05
4
  gene_39
                NA
                                                          4
                                                                        1
                         NA 5.472115e-07 9.259040e-05
5 gene_134
                                                          5
                NA
                                                                        1
                         NA 6.458243e-07 9.259040e-05
                                                          6
                                                                        1
6 gene_27
                NΑ
> table(tcc$estimatedDEG)
```

0 1 851 149

# 5 Generation of simulation data

## 5.1 Introduction and basic usage

As demonstrated in our previous study (Kadota et al., 2012), the DEGES-based normalization methods implemented in **TCC** theoretically outperform the other normalization methods when the numbers of DEGs (G1 vs. G2) in the tag count data are biased. However, it is difficult to determine whether the up- and down-regulated DEGs in one of the groups are actually biased in their number when analyzing real data (Dillies et al., 2012). This means we have to evaluate the potential performance of our DEGES-based methods using mainly simulation data. The simulateReadCounts function generates simulation data under various conditions. This function can generate simulation data analyzed in the TbT paper (Kadota et al., 2012), and that means it enables other researchers to compare the methods they develop with our DEGES-based methods. For example, the hypoData object, a hypothetical count dataset provided in **TCC**, was generated by using this function. The output of the simulateReadCounts function is stored as a **TCC** class object and is therefore ready-to-analyze.

Note that different trials of simulation analysis generally yield different count data even under the same simulation conditions. We can call the set.seed function in order to obtain reproducible results (i.e., the tcc\$count) with the simulateReadCounts function.

[1] 1000 6

> head(tcc\$count)

		G1_rep1	G1_rep2	G1_rep3	G2_rep1	G2_rep2	G2_rep3
	gene_1	347	65	267	3	14	57
	gene_2	10	114	87	4	4	3
	gene_3	121	44	84	15	17	13
	gene_4	62	18	7	1	19	12
	gene_5	2	4	11	1	3	5
	gene_6	353	338	212	59	50	77

#### > tcc\$group

	group
G1_rep1	1
G1_rep2	1
G1_rep3	1
G2_rep1	2
G2_rep2	2
G2_rep3	2

The simulation conditions for comparing two groups (G1 vs. G2) with biological replicates are as follows: (i) the number of genes is 1,000 (i.e., Ngene = 1000), (ii) the first 20% of genes are DEGs (PDEG = 0.2), (iii) the first 90% of the DEGs are up-regulated in G1, and the remaining 10% are up-regulated in G2 (DEG.assign = c(0.9, 0.1)), (iv) the levels of DE are four-fold in both groups (DEG.foldchange = c(4, 4)), and (v) there are a total of six samples (three biological replicates for G1 and three biological replicates for G2) (replicates = c(3, 3)). The variance of the NB distribution can be modeled as  $V = \mu + \phi \mu^2$ . The empirical distribution of the read counts for producing the mean ( $\mu$ ) and dispersion ( $\phi$ ) parameters of the model was obtained from *Arabidopsis* data (three biological replicates for each of the treated and non-treated groups) in NBPSeq (Di et al., 2011).

The tcc\$count object is essentially the same as the hypoData object of TCC. The information about the simulation conditions can be viewed as follows.

### > str(tcc\$simulation)

```
List of 4
$ trueDEG : Named num [1:1000] 1 1 1 1 1 1 1 1 1 1 1 1 ...
..- attr(*, "names")= chr [1:1000] "gene_1" "gene_2" "gene_3" "gene_4" ...
$ DEG.foldchange: num [1:1000, 1:6] 4 4 4 4 4 4 4 4 4 4 4 ...
..- attr(*, "dimnames")=List of 2
....$ : chr [1:1000] "gene_1" "gene_2" "gene_3" "gene_4" ...
$ ....$ : chr [1:6] "G1_rep1" "G1_rep2" "G1_rep3" "G2_rep1" ...
$ PDEG : num [1:2] 0.18 0.02
$ params :'data.frame': 1000 obs. of 2 variables:
...$ mean: num [1:1000] 30.82 14.06 16.98 12.97 1.94 ...
...$ disp: num [1:1000] 0.8363 1.8306 0.0962 0.5087 0.5527 ...
```

Specifically, the entries for 0 and 1 in the tcc\$simulation\$trueDEG object are for non-DEGs and DEGs respectively. The breakdowns for individual entries are the same as stated above: 800 entries are non-DEGs, 200 entries are DEGs.

```
> table(tcc$simulation$trueDEG)
```

### 0 1 800 200

This information can be used to evaluate the performance of the DEGES-based normalization methods in terms of the sensitivity and specificity of the results of their DE analysis. A good normalization method coupled with a DE method such as the exact test (Robinson and Smyth, 2008) and the empirical Bayes (Hardcastle and Kelly, 2010) should produce well-ranked gene lists in which the true DEGs are top-ranked and non-DEGs are bottomranked when all genes are ranked according to the degree of DE. The ranked gene list after performing the DEGES/edgeR-edgeR combination can be obtained as follows.

```
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 1, FDR = 0.1, floorPDEG = 0.05)
> tcc <- estimateDE(tcc, test.method = "edger", FDR = 0.1)
> result <- getResult(tcc, sort = TRUE)
> head(result)
```

	gene_id	a.value	m.value	p.value	q.value	rank	estimatedDEG
1	gene_63	10.935941	-2.161512	7.832711e-07	0.0007452548	1	1
				2.078328e-06			1
3	gene_83	12.299866	-1.885649	2.235764e-06	0.0007452548	3	1
4	gene_57	11.525330	-1.967154	3.086287e-06	0.0007715718	4	1
5	gene_23	8.701215	-2.128781	8.490098e-06	0.0013570693	5	1
6	gene_118	8.717161	-2.174181	9.293293e-06	0.0013570693	6	1

We can now calculate the area under the **ROC** curve (i.e., AUC;  $0 \leq AUC \leq 1$ ) between the ranked gene list and the truth (i.e., DEGs or non-DEGs) and thereby evaluate the sensitivity and specificity simultaneously. A well-ranked gene list should have a high AUC value (i.e., high sensitivity and specificity). The calcAUCValue function calculates the AUC value based on the information stored in the **TCC** class object.

```
> calcAUCValue(tcc)
```

### [1] 0.9131938

This is essentially the same as

### [1] 0.9131938

The following classic **edgeR** procedure (i.e., the TMM-edgeR combination) make it clear that the DEGES-based normalization method (i.e., the DEGES/edgeR pipeline) outperforms the default normalization method (i.e., TMM) implemented in **edgeR**.

```
> tcc <- calcNormFactors(tcc, norm.method = "tmm", iteration = 0)
> tcc <- estimateDE(tcc, test.method = "edger", FDR = 0.1)
> calcAUCValue(tcc)
```

[1] 0.8972625

The following is an alternative procedure for **edgeR** users.

```
> design <- model.matrix(~ as.factor(tcc$group$group))
> d <- DGEList(counts = tcc$count, group = tcc$group$group)
> d <- calcNormFactors(d)
> d$samples$norm.factors <- d$samples$norm.factors /
+ mean(d$samples$norm.factors)
> d <- estimateDisp(d, design)
> fit <- glmQLFit(d, design)
> result <- glmQLFTest(fit, coef = 2)
> result$table$PValue[is.na(result$table$PValue)] <- 1
> AUC(rocdemo.sca(truth = as.numeric(tcc$simulation$trueDEG != 0),
+ data = -rank(result$table$PValue)))
```

[1] 0.8972625

# 5.2 Multi-group data with and without replicates

The simulateReadCounts function can generate simulation data with a more complex design. First, we generate a dataset consisting of three groups. The simulation conditions for this dataset are as follows: (i) the number of genes is 1,000 (i.e., Ngene = 1000), (ii) the first 30% of genes are DEGs (PDEG = 0.3), (iii) the breakdowns of the up-regulated DEGs are respectively 70%, 20%, and 10% in Groups 1-3 (DEG.assign = c(0.7, 0.2, 0.1)), (iv) the levels of DE are 3-, 10-, and 6-fold in individual groups (DEG.foldchange = c(3, 10, 6)), and (v) there are a total of nine libraries (2, 4, and 3 replicates for Groups 1-3) (replicates = c(2, 4, 3)).

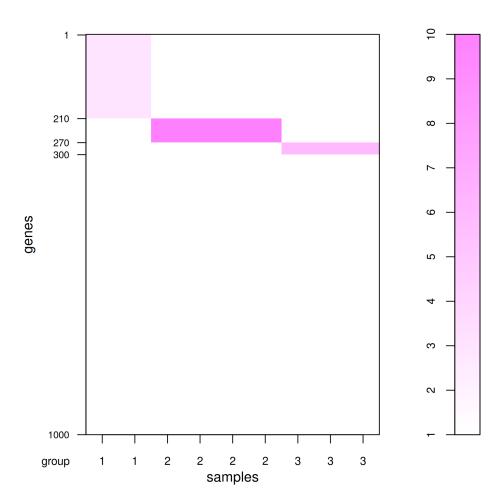
```
> set.seed(1000)
> library(TCC)
> tcc <- simulateReadCounts(Ngene = 1000, PDEG = 0.3,</pre>
                             DEG.assign = c(0.7, 0.2, 0.1),
                             DEG.foldchange = c(3, 10, 6),
                             replicates = c(2, 4, 3))
> dim(tcc$count)
[1] 1000
             9
> tcc$group
        group
G1_rep1
             1
G1_rep2
             1
             2
G2_rep1
             2
G2_rep2
             2
G2_rep3
G2_rep4
            2
             3
G3_rep1
            3
G3_rep2
            3
G3_rep3
```

### > head(tcc\$count)

	G1_rep1	G1_rep2	G2_rep1	G2_rep2	G2_rep3	G2_rep4	G3_rep1	G3_rep2	G3_rep3
gene_1	259	63	37	5	24	12	4	66	3
gene_2	8	12	2	13	47	2	0	22	24
gene_3	92	64	23	14	18	18	23	20	20
gene_4	48	43	14	24	9	12	6	8	5
gene_5	2	6	4	3	2	0	7	5	0
gene_6	264	237	81	82	73	60	38	87	108

The pseudo-color image for the generated simulation data regarding the DEGs can be obtained from the plotFCPseudocolor function. The right bar (from white to magenta) indicates the degree of fold-change (FC). As expected, it can be seen that the first 210, 60, and 30 genes are up-regulated in G1, G2, and G3, respectively.

### > plotFCPseudocolor(tcc)



Now let us see how the DEGES/edgeR-edgeR combination with the original edgeR-edgeR combination performs. First we calculate the AUC value for the ranked gene list obtained from the DEGES/edgeR-edgeR combination.

```
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 1)
> tcc <- estimateDE(tcc, test.method = "edger", FDR = 0.1)
> calcAUCValue(tcc)
```

### [1] 0.8791524

Next, we calculate the corresponding value using the original **edgeR** procedure for single factor experimental design (i.e., the edgeR-edgeR combination).

```
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 0)
> tcc <- estimateDE(tcc, test.method = "edger", FDR = 0.1)
> calcAUCValue(tcc)
```

### [1] 0.8642762

It can be seen that the DEGES/edgeR-edgeR combination outperforms the original **edgeR** procedure under the given simulation conditions. Note that the **test.method** argument will be ignored when **iteration** = 0 is specified.

Next, let us generate another dataset consisting of a total of eight groups. The simulation conditions for this dataset are as follows: (i) the number of genes is 10,000 (i.e., Ngene = 10000), (ii) the first 34% of genes are DEGs (PDEG = 0.34), (iii) the breakdowns of the up-regulated DEGs are respectively 10%, 30%, 5%, 10%, 5%, 21%, 9%, and 10% in Groups 1-8 (DEG.assign = c(0.1, 0.3, 0.05, 0.1, 0.05, 0.21, 0.09, 0.1)), (iv) the levels of DE are 3.1-, 13-, 2-, 1.5-, 9-, 5.6-, 4-, and 2-fold in individual groups (DEG.foldchange = c(3.1, 13, 2, 1.5, 9, 5.6, 4, 2)), and (v) there are a total of nine libraries (except for G3, none of the groups have replicates) (replicates = c(1, 1, 2, 1, 1, 1, 1)).

```
> set.seed(1000)
> library(TCC)
> tcc <- simulateReadCounts(Ngene = 10000, PDEG = 0.34,
+ DEG.assign = c(0.1, 0.3, 0.05, 0.1, 0.05, 0.21, 0.09, 0.1),
+ DEG.foldchange = c(3.1, 13, 2, 1.5, 9, 5.6, 4, 2),
+ replicates = c(1, 1, 2, 1, 1, 1, 1))
> dim(tcc$count)
```

```
[1] 10000
```

9

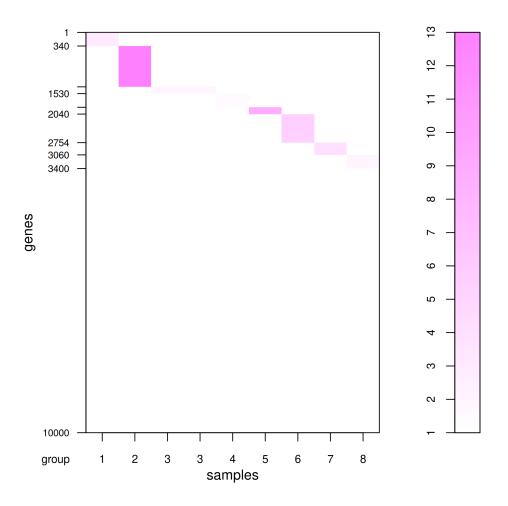
> tcc\$group

group G1\_rep1 1 G2\_rep1 2 G3\_rep1 3 G3\_rep2 3 G4\_rep1 4 G5\_rep1 5 G6\_rep1 6 G7\_rep1 7 G8\_rep1 8

> head(tcc\$count)

	G1_rep1	G2_rep1	G3_rep1	G3_rep2	G4_rep1	G5_rep1	G6_rep1	G7_rep1	G8_rep1
gene_1	16	16	14	63	16	62	64	42	9
gene_2	2	0	24	10	3	22	14	40	3
gene_3	72	27	25	17	20	20	10	20	12
gene_4	32	16	6	7	18	6	1	0	22
gene_5	0	1	6	0	2	0	4	1	8
gene_6	327	182	172	158	107	87	72	147	76

### > plotFCPseudocolor(tcc)



This kind of simulation data may be useful for evaluating methods aimed at identifying tissue-specific (or tissue-selective) genes.

### 5.3 Multi-factor data

The simulateReadCounts function can also generate simulation data in multi-factor experimental design. Different from above single-factor experimental design, the group argument should be used instead of replicates for specifying sample conditions (or factors) when generating simulation data in multi-factor design. In relation to the group specification, the DEG.foldchange argument should also be specified as a data frame object.

We generate a dataset consisting of two factors for comparing (i) two Groups (i.e., "WT" vs. "KO") as the first factor, at (ii) two time points (i.e., "1d" vs. "2d") as the second factor, with all samples obtained from independent subjects. There are a total of four conditions ("WT\_1d", "WT\_2d", "KO\_1d", and "KO\_2d") each of which has two biological replicates, comprising a total of eight samples. The group argument for this experimental design can be described as follows:

```
> group <- data.frame(
+ GROUP = c("WT", "WT", "WT", "KO", "KO", "KO", "KO", "KO"),
+ TIME = c("1d", "1d", "2d", "2d", "1d", "1d", "2d", "2d")
+ )</pre>
```

Next, we design the number of types of DEGs and the levels of fold-change by the DEG.foldchange argument. We here introduce three types of DEGs: (a) 2-fold up-regulation in the first four samples (i.e., "WT"), (b) 3-fold up-regulation in the last four samples (i.e., "KO"), and (c) 2-fold down-regulation at "2d" in "WT" and 4-fold up-regulation at "2d" in "KO". This implies that the first two types of DEGs are related to the first factor (i.e., "WT" vs. "KO") and the third type of DEG is related to the second factor (i.e., "1d" vs. "2d").

```
> DEG.foldchange <- data.frame(
+ FACTOR1.1 = c(2, 2, 2, 2, 1, 1, 1, 1),
+ FACTOR1.2 = c(1, 1, 1, 1, 3, 3, 3, 3),
+ FACTOR2 = c(1, 1, 0.5, 0.5, 1, 1, 4, 4)
+ )
```

The other simulation conditions for this dataset are as follows: (1) the number of gene is 1,000 (i.e., Ngene = 1000), (2) the first 20% of genes are DEGs (i.e., PDEG = 0.2), and (3) the breakdowns of the three types of DEGs are 50%, 20%, and 30% (i.e., DEG.assign = c(0.5, 0.2, 0.3)).

Since the first six rows in the dataset corresponds to the first type of DEGs, we can see the 2-fold up-regulation in the first four columns (i.e., WT-related samples) compared to the last four columns (i.e., KO-related samples).

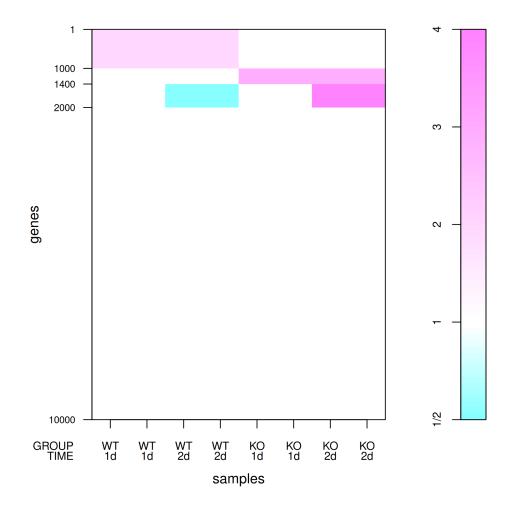
### > head(tcc\$count)

	WT1d_rep1	WT1d_rep2	WT2d_rep1	WT2d_rep2	KO1d_rep1	KO1d_rep2	KO2d_rep1
gene_1	12	33	14	130	39	4	40
gene_2	14	23	1	19	13	2	2
gene_3	21	64	26	27	11	16	10
gene_4	12	36	47	10	8	15	16
gene_5	2	0	1	2	1	4	0
gene_6	174	110	197	115	58	30	69
-	KO2d_rep2						
gene_1	42						
gene_2	40						
gene_3	20						
gene_4	0						
gene_5	1						
gene_6	147						

> tcc\$group

	GROUP	TIME
WT1d_rep1	WT	1d
WT1d_rep2	WT	1d
WT2d_rep1	WT	2d
WT2d_rep2	WT	2d
KO1d_rep1	KO	1d
KO1d_rep2	KO	1d
KO2d_rep1	KO	2d
KO2d_rep2	KO	2d

### > plotFCPseudocolor(tcc)



# 5.4 Other utilities

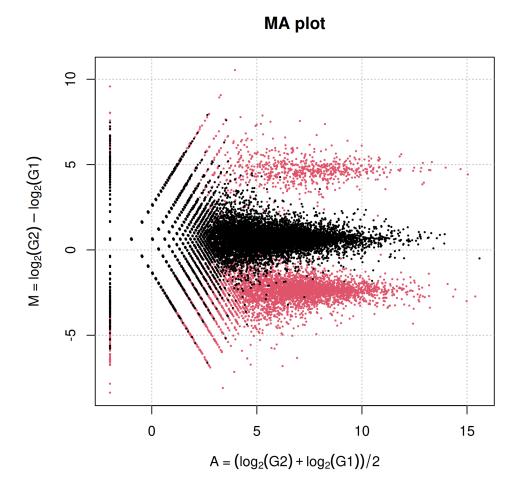
Recall that the simulation framework can handle different levels of DE for DEGs in individual groups, and the shape of the distribution for these DEGs is the same as that of non-DEGs. Let us confirm those distributions by introducing more drastic simulation conditions for comparing two groups (G1 vs. G2) with biological replicates; i.e., (i) the number of genes is 20,000 (i.e., Ngene = 20000), (ii) the first 30% of genes are DEGs (PDEG = 0.30), (iii) the first 85% of the DEGs are up-regulated in G1 and the remaining 15% are up-regulated in G2 (DEG.assign = c(0.85, 0.15)), (iv) the levels of DE are eight-fold in G1 and sixteenfold in G2 (DEG.foldchange = c(8, 16)), and (v) there are a total of four samples (two biological replicates for G1 and two biological replicates for G2) (replicates = c(2, 2)).

```
> set.seed(1000)
 library(TCC)
>
>
  tcc <- simulateReadCounts(Ngene = 20000, PDEG = 0.30,</pre>
                  DEG.assign = c(0.85, 0.15),
+
+
                  DEG.foldchange = c(8, 16),
                  replicates = c(2, 2))
+
>
 head(tcc$count)
       G1_rep1 G1_rep2 G2_rep1 G2_rep2
                              0
gene_1
          415
                    238
                                     140
```

gene_2	0	73	0	9
gene_3	148	110	10	31
gene_4	134	189	28	3
gene_5	32	18	1	0
gene_6	467	363	93	53

An M-A plot for the simulation data can be viewed as follows; the points for DEGs are colored red and the non-DEGs are colored black:

### > plot(tcc)



This plot is generated from simulation data that has been scaled in such a way that the library sizes of each sample are the same as the mean library size of the original data. That is,

```
> normalized.count <- getNormalizedData(tcc)
> colSums(normalized.count)
G1_rep1 G1_rep2 G2_rep1 G2_rep2
```

```
4155848 4155848 4155848 4155848
```

```
> colSums(tcc$count)
```

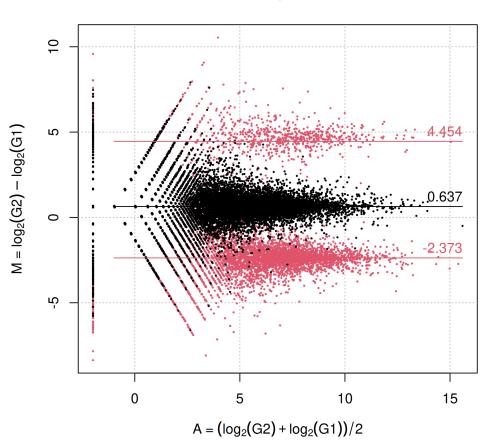
```
G1_rep1 G1_rep2 G2_rep1 G2_rep2
4954709 5152169 3226887 3289627
```

```
> mean(colSums(tcc$count))
```

[1] 4155848

The summary statistics for non-DEGs and up-regulated DEGs in G1 and G2 are upshifted compared with the original intentions of the user (i.e., respective M values of 0, -3, and 4 for non-DEGs and up-regulated DEGs in G1 and G2). Indeed, the median values, indicated as horizontal lines, are respectively 0.637, -2.373, and 4.454 for non-DEGs and up-regulated DEGs in G1 and G2.

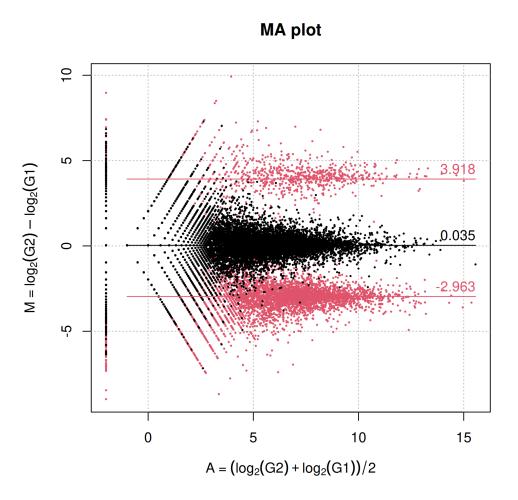
> plot(tcc, median.lines = TRUE)



MA plot

These upshifted M values for non-DEGs can be modified after performing the iDEGES/edgeR normalization, e.g., the median M value (= 0.035) for non-DEGs based on the iDEGES/edgeR-normalized data is nearly zero.

```
> tcc <- calcNormFactors(tcc, norm.method = "tmm", test.method = "edger",
+ iteration = 3, FDR = 0.1, floorPDEG = 0.05)
> plot(tcc, median.line = TRUE)
```



The comparison of those values obtained from different normalization methods might be another evaluation metric.

# 6 Session info

> sessionInfo()

R version 4.4.1 (2024-06-14) Platform: x86\_64-pc-linux-gnu Running under: Ubuntu 24.04.1 LTS Matrix products: default /home/biocbuild/bbs-3.20-bioc/R/lib/libRblas.so BLAS: LAPACK: /usr/lib/x86\_64-linux-gnu/lapack/liblapack.so.3.12.0 locale: [1] LC\_CTYPE=en\_US.UTF-8 LC\_NUMERIC=C [3] LC\_TIME=en\_GB LC\_COLLATE=C [5] LC\_MONETARY=en\_US.UTF-8 LC\_MESSAGES=en\_US.UTF-8 [7] LC\_PAPER=en\_US.UTF-8 LC\_NAME=C [9] LC\_ADDRESS=C LC\_TELEPHONE=C [11] LC\_MEASUREMENT=en\_US.UTF-8 LC\_IDENTIFICATION=C time zone: America/New\_York tzcode source: system (glibc) attached base packages: [1] stats4 stats graphics grDevices utils datasets methods [8] base other attached packages: [1] TCC\_1.46.0 ROC\_1.82.0 [3] edgeR\_4.4.0 limma\_3.62.0 [5] DESeq2\_1.46.0 SummarizedExperiment\_1.36.0 MatrixGenerics\_1.18.0 [7] Biobase\_2.66.0 [9] matrixStats\_1.4.1 GenomicRanges\_1.58.0 IRanges\_2.40.0 [11] GenomeInfoDb\_1.42.0 BiocGenerics\_0.52.0 [13] S4Vectors\_0.44.0 loaded via a namespace (and not attached): 

 [1] utf8\_1.2.4
 generics\_0.1.3

 [4] lattice\_0.22-6
 magrittr\_2.0.3

 [7] jsonlite\_1.8.9
 Matrix\_1.7-1

 [10] fansi\_1.0.6
 UCCC

 SparseArray\_1.6.0 grid\_4.4.1 httr\_1.4.7 
 Matrix\_1.7-1
 Mode\_\_\_

 UCSC.utils\_1.2.0
 scales\_1.3.0

 shind 1 4-8
 cli\_3.6.3

 Cli\_shind 1 4-8
 cli\_shind 1 4-8
 [10] fansi\_1.0.6 abind\_1.4-8 cli\_3.6.3 crayon\_1.5.3 XVector\_0.46.0 DelayedArray\_0.32.0 S4Arrays\_1.6.0 parallel\_4.4.1 BiocParallel\_1.40.0 colorspace\_2.1-1 ggplot2\_3.5.1 GenomeInfoDbData\_1.2.13 vctrs\_0.6.5 [13] codetools\_0.2-20 [16] rlang\_1.1.4 [19] munsell\_0.5.1 [22] tools\_4.4.1 [25] dplyr\_1.1.4 [28] locfit\_1.5-9.10 lifecycle\_1.0.4 zlibbioc\_1.52.0 pillar\_1.9.0 gtable\_0.3.6 Rcpp\_1.0.13 statmod\_1.5.0 [31] R6\_2.5.1 pillar\_1.9.0 Rcpp\_1.0.13 [34] pkgconfig\_2.0.3 [37] glue\_1.8.0 [40] xfun\_0.48 tibble\_3.2.1 tidyselect\_1.2.1 [43] knitr\_1.48 compiler\_4.4.1

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